## Marcus theory for electron transfer kinetics

CCB 341: Physical Chemistry of biochemical systems, Fall 2013



The potential energies as a function of the "distortion coordinate" q are:

$$V_A(q) = \frac{1}{2}k(q - q_A)^2$$
  $V_B(q) = \frac{1}{2}k(q - q_B)^2 + \Delta E$ 

Or

$$V_B - V_A = \Delta V(q) = -k(q - q_A) \left(\frac{2\lambda}{k}\right)^{1/2} + \lambda + \Delta E$$

Now we can find the point  $q^*$  where  $\Delta V(q^*) = 0$ :

$$(q^*-q_A)=rac{(\lambda+\Delta E)}{(2\lambda k)^{1/2}}=rac{\lambda(1+\Delta E/\lambda)}{(2\lambda k)^{1/2}}$$

Next, we can compute the activation energy, which is the value of  $V_A(q^*)$ :

$$V_A(q^*) = \frac{1}{2}k(q^* - q_A)^2 = \frac{1}{2}k\frac{\lambda^2(1 + \Delta E/\lambda)^2}{(2\lambda k)} = \frac{\lambda}{4}\left(1 + \frac{\Delta E}{\lambda}\right)^2$$

This last is Eq. (9.53) in your text. Note that terms in k cancel.