

Molecular simulations of biomolecules
Remote Lecture #8
thermodynamic cycles
connections to experimental restraints

CCB 550, Spring 2020

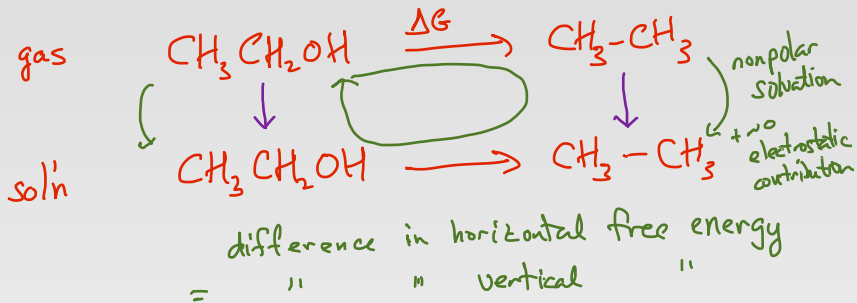
Types of thermodynamic calculations

- “alchemical” changes: $V_0 \rightarrow V_1$, using TI or FEP
 - end states can have different chemistry; or different environments; or just different force fields
- conformational free energy changes: using umbrella sampling or other enhanced sampling techniques
- “end-point” methods:

$$G \simeq \langle H_{MM} \rangle - TS_{chain} + \langle \Delta G_{solvation} \rangle$$

Thermodynamic cycles: transfer free energies

- See Fig. 12.3 in your text



Thermodynamic cycles:

- See Figs. 11.9, 11.10 in your text

Thermodynamic cycles: pH and redox behavior

- See Fig. 12.4 in your text

Bayes theorem in probability theory

$$p(A \cap B) = p(A|B)p(B) = p(B \cap A) = p(B|A)p(A) \quad (1)$$

$$p(A|B) = \frac{p(B|A)p(A)}{p(B)}$$

- Nomenclature (jargon): $p(A)$ is the “prior” estimate of the likelihood that A is true; $p(A|B)$ is the “posterior” estimate of likelihood, given evidence B
- philosophy of probabilities: frequentist interpretation vs. Bayesian (“degree of belief”) interpretation

Using force fields instead of conventional geometric restraints

$$p(\text{model}|\text{data}) = \frac{p(\text{data}|\text{model})p(\text{model})}{p(\text{data})}$$

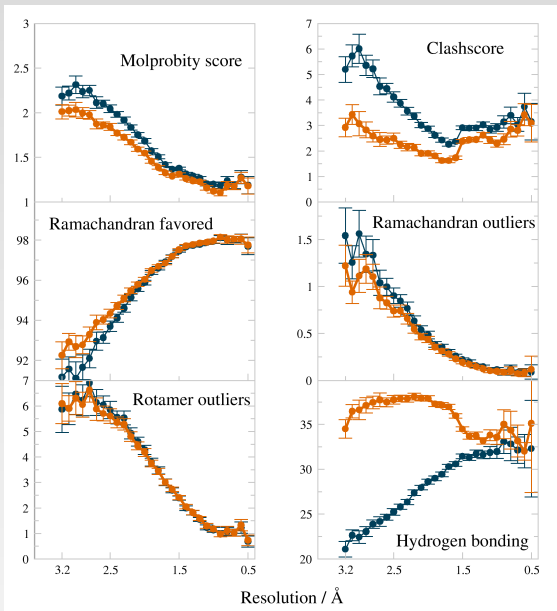
$-\ln[p(\text{data}|\text{model})] = \text{ML target}; \quad -\ln[p(\text{model})] \approx E_{MM}/k_B T_{\text{eff}}$

- Why would one want to do this? Or think it might work?
 - provides an approach to correlations among restraints; suggests a rational way to decide how much weight bonds vs. angles vs. clashes vs. torsions....
 - useful when restraints are hard to obtain via small molecule databases
 - a force field energy (eventually?) should optimally encode our prior knowledge about structure
 - especially at low resolution, energies should provide more restrictive restraints than simple geometric restraints

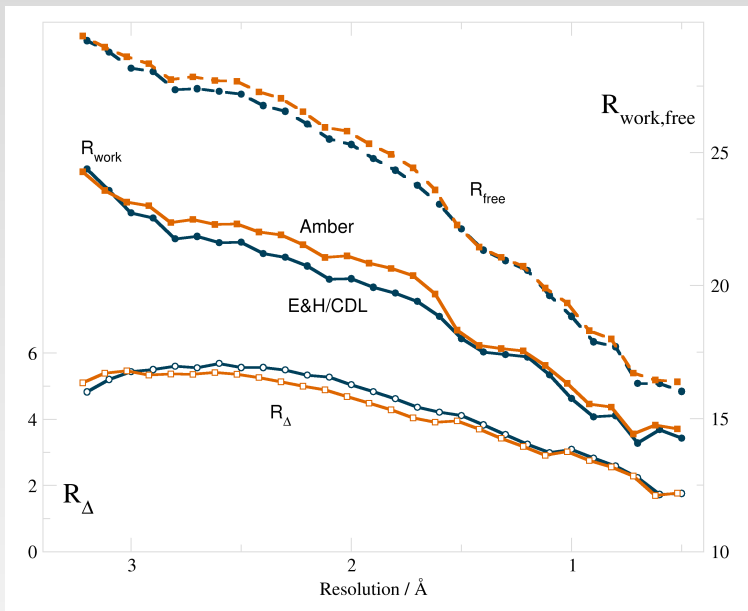
Wait: hasn't this all been done before?

- XPLOR (e.g. Karplus & Brünger, *Acc. Chem. Res.* 24:54, 1991); CNS; FFX (Schnieders, Fenn, Pande, Brünger, *Acta Cryst D* 65:952, 2009); PrimeX, QuantumBio, OpenEye, others....
- What can be done now, by someone with no Amber experience?
- `phenix.AmberPrep 9xyz.pdb <options>`
- `phenix.refine 4phenix_9xyz.pdb use_amber=True
topology_file_name=4amber_9xyz.prmtop
amber.coordinate_file_name=4amber_9xyz.rst7
amber.order_file_name=4amber_9xyz.order`

Results from 13,237 paired protein refinements



Results from 13,237 paired protein refinements



Molecular dynamics-based structure refinement

Fundamentals of MD refinement

$$E(\underline{x}) = E^{MM}(\underline{x}) + \sum K (d - d^0)^2$$

prior idea general info about proteins

K for typical covalent bond

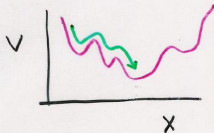
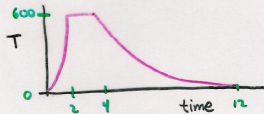
noe constraints

500 kcal/mol \AA^{-2}

K_{noe} = ?? values from 1-40 are used.

$$-\frac{\partial E}{\partial \underline{x}} \equiv \underline{F} = m \ddot{\underline{x}}$$

integrate numerically, $\frac{3}{2} NkT = \text{K.E.}$



$p(\text{data} | \text{model})$

$p(\text{model} | \text{data})$

outcome of a refinement