

Molecular simulations of biomolecules  
Remote Lecture #8  
thermodynamic cycles  
connections to experimental restraints

CCB 550, Spring 2020

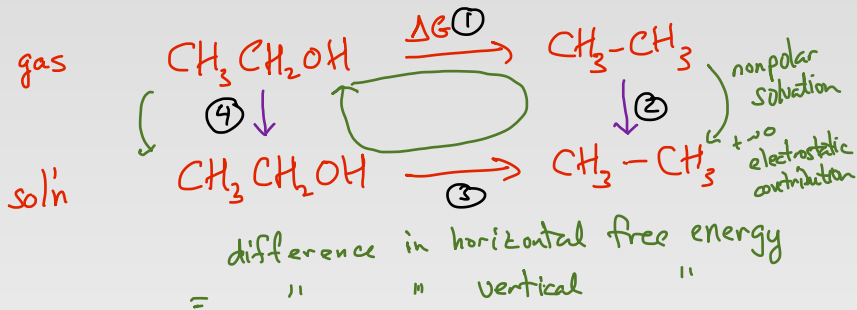
# Types of thermodynamic calculations

- “alchemical” changes:  $V_0 \rightarrow V_1$ , using TI or FEP
  - end states can have different chemistry; or different environments; or just different force fields
- conformational free energy changes: using umbrella sampling or other enhanced sampling techniques
- “end-point” methods:

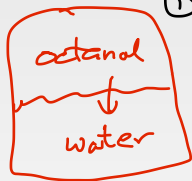
$$G \simeq \langle H_{MM} \rangle - TS_{chain} + \langle \Delta G_{solvation} \rangle$$

# Thermodynamic cycles: transfer free energies

- See Fig. 12.3 in your text



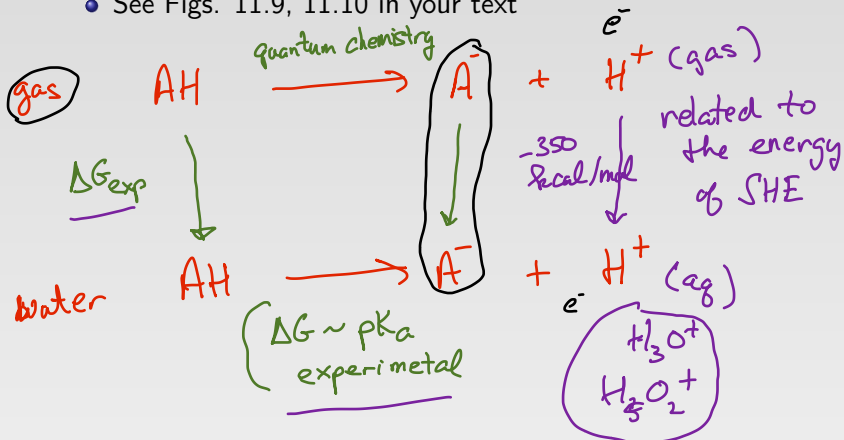
$$(1) + (2) + (3) = (4)$$



partition coefficient

# Thermodynamic cycles:

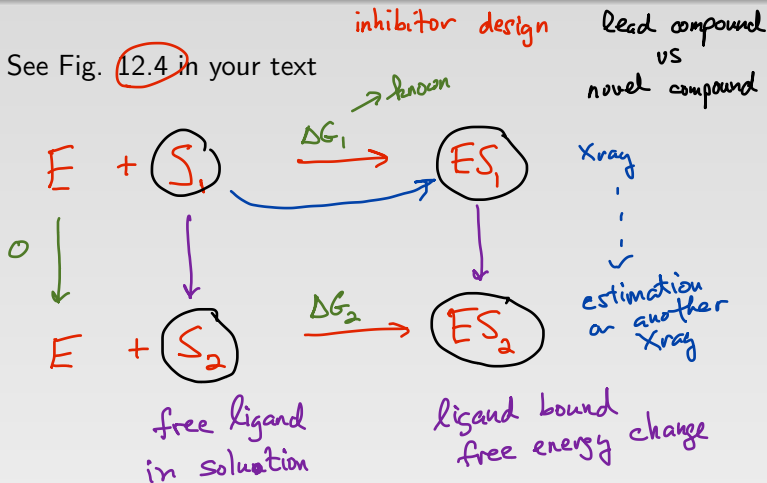
- See Figs. 11.9, 11.10 in your text



- ① want simulations to give right answer because ~~we~~ we want to simulate polar → non-polar

# Thermodynamic cycles: ~~pH and redox behavior~~

- See Fig. 12.4 in your text



① alchemy: two purple arrows

② umbrella sampling: two horizontal lines

more recently  
gaining attention

# Bayes theorem in probability theory

$$p(A \cap B) = p(A|B)p(B) = p(B \cap A) = p(B|A)p(A) \quad (1)$$

*conditional probability*

*prob. that both A and B are true*

*posterior likelihood*

$$p(A|B) = \frac{p(B|A)p(A)}{p(B)}$$

*prior*

- Nomenclature (jargon):  $p(A)$  is the “prior” estimate of the likelihood that  $A$  is true;  $p(A|B)$  is the “posterior” estimate of likelihood, given evidence  $B$
- philosophy of probabilities: frequentist interpretation vs. Bayesian (“degree of belief”) interpretation

*B represents additional information*

# Using force fields instead of conventional geometric restraints

construct a model that

maximize  $\xi$  this

$$p(\text{model}|\text{data})$$

$$= \frac{p(\text{data}|\text{model}) p(\text{model})}{p(\text{data})}$$

$p(\text{data}) \rightarrow$  fixed constant

$$-\ln[p(\text{data}|\text{model})] = \text{ML target}, \quad -\ln[p(\text{model})] \approx E_{MM}/k_B T_{\text{eff}}$$

- Why would one want to do this? Or think it might work?
  - provides an approach to correlations among restraints; suggests a rational way to decide how much weight bonds vs. angles vs. clashes vs. torsions....
  - useful when restraints are hard to obtain via small molecule databases
  - a force field energy (eventually?) should optimally encode our prior knowledge about structure
  - especially at low resolution, energies should provide more restrictive restraints than simple geometric restraints

get best model: minimize  $\sum_i (F_i^{\text{calc}} - F_i^{\text{obs}})^2$

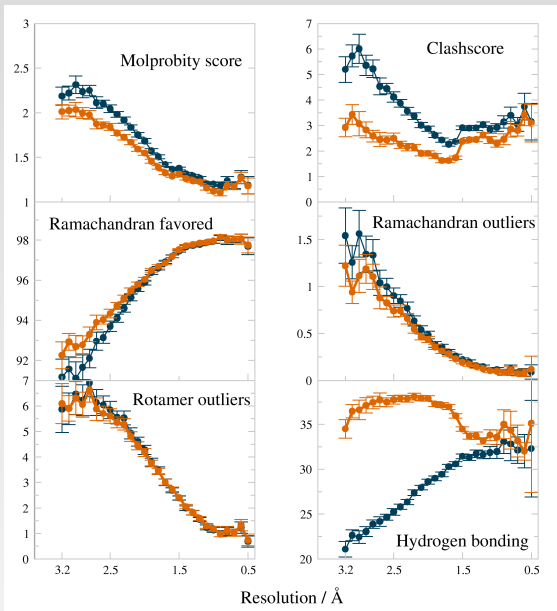
$$\left( \frac{E_{MM}}{k_B T} \right)_{\text{natural}} + \text{ML target} + \text{artificial term}$$

# Wait: hasn't this all been done before?

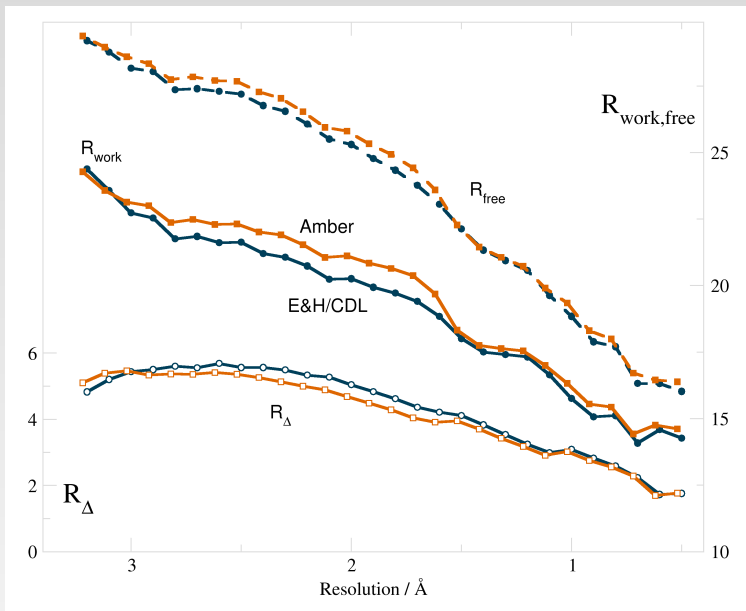
- XPLOR (e.g. Karplus & Brünger, Acc. Chem. Res. 24:54, 1991); CNS; FFX (Schnieders, Fenn, Pande, Brünger, Acta Cryst D 65:952, 2009); PrimeX, QuantumBio, OpenEye, others....
- What can be done now, by someone with no Amber experience?
- `phenix.AmberPrep 9xyz.pdb <options>`
- `phenix.refine 4phenix_9xyz.pdb use_amber=True  
topology_file_name=4amber_9xyz.prmtop  
amber.coordinate_file_name=4amber_9xyz.rst7  
amber.order_file_name=4amber_9xyz.order ....`



# Results from 13,237 paired protein refinements



# Results from 13,237 paired protein refinements



# Molecular dynamics-based structure refinement

## Fundamentals of MD refinement

$$E(\underline{x}) = E^{MM}(\underline{x}) + \sum K(d-d^u)^2$$

$K$  for typical covalent bond 500 kcal/mol  $\text{\AA}^{-2}$

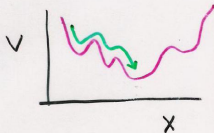
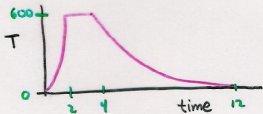
prior idea  
general info  
about proteins

$K_{noe} = ??$  values from 1-40 are used.

weighting  
between  
 $E^{MM}$   
and  
data-driven  
constraints

$$-\frac{\partial E}{\partial \underline{x}} \equiv \underline{F} = m \ddot{\underline{x}}$$

integrate numerically,  $\frac{3}{2} NkT = \text{K.E.}$



$p(\text{data} | \text{model})$

$p(\text{model} | \text{data})$

outcome of  
a refinement

estimates  
distances  
between  
nuclei

there is a  
range of  $K$   
that give  
almost the  
same answer